

A Relational Model of Data for Large Shared Data Banks (Original Manuscript)

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This is the first installment. Section 2 will be available next week.

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Abstract

Future users of large data banks must be protected from having to know how the data is organized in the machine (the internal representation). A prompting service which supplies such information is not a satisfactory solution. Activities of users at terminals and most application programs should remain unaffected when the internal representation of data is changed and even when some aspects of the external representation are changed.

Changes in data representation will often be needed as a result of changes in query, update, and report traffic and natural growth in the types of stored information.

Existing non inferential, formatted data systems provide users with tree-structured files or slightly more general network models of the data. In [Section 1](#), inadequacies of these models are discussed. A model based on n -ary relations, a normal form for data base relations, and the concept of a universal data sub language are introduced. In Section 2,

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certain operations on relations (other than logical inference) are discussed and applied to the problems of redundancy and consistency in the user's model.

Key Words and Phrases

data bank, data base, data structure, data organization;, hierarchies of data, network of data, relations, derivability, redundancy, consistency, composition, join, retrieval language, predicate calculus, security, data integrity

CR Categories

3.70, 3.73, 3.75, 4 20, 4.22, 4.29

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4. [1. Relational Model and Normal Form](#)

1.1 Introduction

This paper is concerned with the application of elementary relation theory to systems which provide shared access to large banks of formatted data. Except for a paper by [Childs \[1\]](#), the principal application of relations to data systems has been to deductive question - answering systems. [Levein and Maron \[2\]](#) provide numerous references to work in this area.

In contrast, the problems treated here are those of data independence - the independence of application programs and terminal activities from growth in data types and changes in data representation and certain kinds of data inconsistency which are expected to become troublesome even in nondeductive systems.

The relational view (or model) of data described in Section 1 appears to be superior in several respects to the graph or network model [\[3, 4\]](#) presently in vogue for non-inferential systems. It provides a means of describing data with its natural structure only -- that is, without superimposing any additional structure for machine representation poses.

Accordingly, it provides a basis for a high level data language which will yield maximal independence between programs on the one hand and machine representation and organization of data on the other.

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A further advantage of the relational view is that it forms a sound basis for treating derivability, redundancy, and consistency of relations - these are discussed in Section 2.

The network model, on the other hand, has spawned a number of confusions, not the least of which is mistaking the derivation of connections for the derivation of relations (see remarks in Section 2 on the "connection trap").

Finally, the relational view permits a clearer evaluation of the scope and logical limitations of present formatted data systems, and also the relative merits (from a logical standpoint) of competing representations of data within a single system. Examples of this clearer perspective are cited in various parts of this paper. Implementations of systems to support the relational model are not discussed.

1.2 Data Dependence in Present Systems

The provision of data description tables in recently developed information systems represents a major advance toward the goal of data independence [5, 6, 7]. Such tables facilitate changing certain characteristics of the data representation stored in a data bank. However, the variety of data representation characteristics which can be changed without logically impairing some application programs is still quite limited. Further, the model of data with which users interact is still cluttered with representational properties, particularly in regard to the representation of collections of data (as opposed to individual items).

Three of the principal kinds of data dependencies which still need to be removed are:

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ordering dependence, indexing dependence, and access path dependence. In some systems these dependencies are not clearly separable from one another.

1.2.1. Ordering Dependence

Elements of data in a data bank may be stored in a variety of ways, some involving no concern for ordering, some permitting each element to participate in one ordering only, others permitting each element to participate in several orderings. Let us consider those existing systems which either require or permit data elements to be stored in at least one total ordering which is closely associated with the hardwired-determined ordering of addresses. For example, the records of a file concerning parts might be stored in ascending order by part serial number. Such systems normally permit application programs to assume that the order of presentation of records from such a file is identical to (or is a subordering of) the stored ordering. Those application programs which take advantage of the stored ordering of a file are likely to fail to operate correctly if for some reason it becomes necessary to replace that ordering by a different one. Similar remarks hold for a stored ordering implemented by means of pointers.

It is unnecessary to single out any system as an example, because all the well-known information systems that are marketed today fail to make a clear distinction between order of presentation on the one hand and stored ordering on the other. Significant implementation problems must be solved to provide this kind of independence.

1.2.2. Indexing Dependence

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In the context of formatted data, an index is usually thought of as a purely performance-oriented component of the data representation. It tends to improve response to queries and updates and, at the same time, slow down response to insertions and deletions. From an informational standpoint, an index is a redundant component of the data representation. If a system uses indices at all and if it is to perform well in an environment with changing patterns of activity on the data bank, an ability to create and destroy indices from time to time will probably be necessary. The question then arises: Can application programs and terminal activities remain invariant as indices come and go?

Present formatted data systems take widely different approaches to indexing. [TDMS \[7\]](#) unconditionally provides indexing on all attributes. The presently released version of [IMS \[5\]](#) provides the user with a choice for each file: a choice between no indexing at all (the hierarchic sequential organization) or indexing on the primary key only (the hierarchic indexed sequential organization). In neither case is the user's application logic dependent on the existence of the unconditionally provided indices. [IDS \[8\]](#), however, permits the file designers to select attributes to be indexed and to incorporate indices into the file structure by means of additional chains. Application programs taking advantage of the performance benefit of these indexing chains must refer to those chains by name. Such programs do not operate correctly if these chains are later removed.

1.2.3. Access Path Dependence

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Many of the existing formatted data systems provide users with tree-structured files or slightly more general network models of the data. Application programs developed to work with these systems tend to be logically impaired if the trees or networks are changed in structure. A simple example follows.

Suppose the data bank contains information about parts and projects. For each part, the part number, part name, part description, quantity-on-hand, and quantity-on-order are recorded. For each project, the project number, project name, project description are recorded. Whenever a project makes use of a certain part, the quantity of that part committed to the given project is also recorded. Suppose that the system requires the user or file designer to declare or define the data in terms of tree structures. Then, any one of the hierarchical structures may be adopted for the information mentioned above (see [Structures 1-5](#)).

Now, consider the problem of printing out the part number, part name, and quantity committed for every part used in the project whose project name is "alpha." The following observations may be made regardless of which available tree-oriented information system is selected to tackle this problem. If a program P is developed for this problem assuming one of the five structures above—that is, P makes no test to determine which structure is in effect - then P will fail on at least three of the remaining structures. More specifically, if P succeeds with [structure 5](#), it will fail with all the others; if P succeeds with [structure 3](#) or [4](#), it will fail with at least [1](#), [2](#), and [5](#); if P succeeds with [1](#) or [2](#), it will fail with at least [3](#), [4](#), and [5](#).

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The reason is simple in each case. In the absence of a test to determine which structure is in effect, P fails because an attempt is made to execute a reference to a nonexistent file (available systems treat this as an error) or no attempt is made to execute a reference to a file containing needed information. The reader who is not convinced should develop sample programs for this simple problem.

Since, in general, it is not practical to develop application programs which test for all tree structuring permitted by the system, these programs fail when a change in structure becomes necessary.

Systems which provide users with a network model of the data run into similar difficulties. In both the tree and network cases, the user (or his program) is required to exploit a collection of user access paths to the data. It does not matter whether these paths are in close correspondence with pointer - (defined paths in the stored representation - in IDS the correspondence is extremely simple, in TDMS it is just the opposite. The consequence, regardless of the stored representation, is that terminal activities and programs become dependent on the continued existence of the user access paths.

One solution to this is to adopt the policy that once a user access path is defined it will not be made obsolete until all application programs using that path have become obsolete. Such a policy is not practical, because the number of access paths in the total model for the community of users of a data bank would eventually become excessively large.

1.3. A Relational View of Data

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The term *relation* is used here in its accepted mathematical sense. Given sets S_1, S_1, \dots, S_n , (not necessarily distinct), R is a relation on these n sets if it is a set of n -tuples each of which has its first element from S_1 , its second element from S_1 , and so on. We shall refer to S_j as the j th domain of R . As defined above, R is said to have degree n . Relations of degree 1 are often called *unary*, degree 2 *binary*, degree 3 *ternary*, and degree n *n*-ary.

For expository reasons, we shall frequently make use of an array representation of relations, but it must be remembered that this particular representation is not an essential part of the relational view being expounded. An array which represents an n -ary relation R has the following properties:

1. Each row represents an n -tuple of R .
2. The ordering of rows is immaterial.
3. All rows are distinct.
4. The ordering of columns is significant - it corresponds to the ordering S_1, S_1, \dots, S_n of the domains on which R is defined (see, however, remarks below on domain-ordered and domain-unordered relations).
5. The significance of each column is partially conveyed by labeling it with the name of the corresponding domain.

The example in [Figure 1](#) illustrates a relation of degree called supply, which reflects the shipments-in-progress of parts from specified suppliers to specified projects in specified quantities.

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supply (supplier part project quantity)

1	2	5	17
1	3	5	23
2	3	7	9
2	7	5	4
4	1	1	12

Figure 1. A relation of degree 4

One might ask: If the columns are labeled by the name of corresponding domains, why should the ordering of columns matter? As the example in [Figure 2](#) shows, two columns may have identical headings (indicating identical domains) but possess distinct meanings with respect to the relation. The relation depicted is called *component*. It is a ternary relation, whose first two domains are called *part* and third domain is called *quantity*. The meaning of *component* (x, y, z) is that part x is an immediate component (or subassembly) of part y , and z units of part x are needed to assemble one unit of part y . It is a relation which plays a critical role in the parts explosion problem.

component	(part	part	quantity
	1	5	9
	2	5	7
	3	5	2

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2	6	12
3	6	3
4	7	1
6	7	1

Figure 2. A relation with two identical domains

It is a remarkable fact that several existing information systems (chiefly those based on tree-structured files) fail to provide data representations for relations which have two or more identical domains. The present version of [IMS/360 \[5\]](#) is an example of such a system.

The totality of data in a data bank may be viewed as a collection of time-varying relations. These relations are of assorted degrees. As time progresses, each n -ary relation may be subject to insertion of additional n -tuples, deletion of, existing ones, and alteration of components of any of its existing n -tuples.

In many commercial, governmental, and scientific data banks, however, some of the relations are of quite high degree (a degree of 30 is not at all uncommon). Users should not normally be burdened with remembering the domain ordering of any relation (for example, the ordering *supplier*, then *part*, then *project*, then *quantity* in the relation *supply*).

Accordingly, we propose that users deal, not with relations which are domain-ordered, but with [relationships](#) which are their domain-unordered counterparts. To accomplish this,

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domains must be uniquely identifiable at least within any given relation, without using position. Thus, where there are two or more identical domains, we require in each case that the domain name be qualified by a distinctive *role name*, which serves to identify the role played by that domain in the given relation. For example, in the relation *component* of [Figure 2](#), the first domain *part* might be qualified by the role name *sub*, and the second by *super*, so that users could deal with the relationship component and its domains - *sub.part* *super.part*, *quantity* - without regard to any ordering between these domains.

To sum up, it is proposed that most users should interact with a relational model of the data consisting of a collection of time-varying relationships (rather than relations). Each user need not know more about any relationship than its name together with the names of its domains (role qualified whenever necessary). [see [note 3](#)] Even this information might be offered in menu style by the system (subject to security and privacy constraints) upon request by the user.

There are usually many alternative ways in which a relational model may be established for a data bank. In order to discuss a preferred way (or normal form, we must first introduce a few additional concepts (active domain, primary key, foreign key, nonsimple domain) and establish some links with terminology currently in use in information systems programming. In the remainder of this paper, we shall not bother to distinguish between relations and relationships except where it appears advantageous to be explicit.

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Consider an example of a data bank which includes relations concerning parts, projects, and suppliers. One relation called *part* is defined on the following domains:

1. part number
2. path name
3. part color
4. part weight
5. quantity on hand
6. quantity on order

and possibly other domains as well. Each of these domains is, in effect, a pool of values, some or all of which may be represented in the data bank at any instant. While it is conceivable that at some instant, all part colors are present, it is unlikely that all possible part weights, part names, and part numbers are. We shall call the set of values represented at some instant the active domain at that instant.

Normally, one domain (or combination of domains) of a given relation has values which uniquely identify each element (n -tuple) of that relation. Such a domain (or combination) is called a *primary key*. In the example above, part number would be a primary key, while part color would not be. A primary key is nonredundant if it is either a simple domain (not a combination) or a combination such that none of the participating simple domains is superfluous in uniquely identifying each element. A relation may possess more than one *nonredundant* primary key. This would be the case in the example if different parts were

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always given distinct names. Whenever a relation has two or more nonredundant primary keys, one of them is arbitrarily selected and called *the* primary key of that relation.

A common requirement is for elements of a relation to cross-reference other elements of the same relation or elements of a different relation. Keys provide a user-oriented means (but not the only means) of expressing such cross-references. We shall call a domain (or domain combination) of relation *R* a *foreign key* if it is not the primary key of *R* but its elements are values of the primary key of some relation *S* (the possibility that *S* and *R* are identical is not excluded). In the relation *supply* of [Figure 1](#), the combination of *supplier*, *part*, *project* is the primary key, while each of these three domains taken separately is a foreign key.

In previous work there has been a strong tendency to treat the data in a data bank as consisting of two parts, one part consisting of entity descriptions (for example, descriptions of suppliers) and the other part consisting of relations between the various entities or types of entities (for example, the *supply* relation). This distinction is difficult to maintain when one may have foreign keys in any relation whatsoever. In the user's relational model there appears to be no advantage to making such a distinction (there may be some advantage, however, when one applies relational concepts to machine representations of the user's set of relationships).

So far, we have discussed examples of relations which are defined on simple domains—domains whose elements are atomic (nondecomposable) values. Nonatomic

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values can be discussed within the relational framework. Thus, some domains may have relations as elements. These relations may, in turn, be defined on nonsimple domains, and so on. For example, one of the domains on which the relation *employee* is defined might be *salary history*. An element of the salary history domain is a binary relation defined on the domain *date* and the domain *salary*. The *salary history* domain is the set of all such binary relations. At any instant of time there are as many instances of the *salary history* relation in the data bank as there are employees. In contrast, there is only one instance of the *employee* relation.

The terms attribute and repeating group in present data base terminology are roughly analogous to simple domain and nonsimple domain, respectively. Much of the confusion in present terminology is due to failure to distinguish between type and instance (as in "record") and between components of a user model of the data on the one hand and their machine representation counterparts on the other hand (again, we cite "record" as an example).

1.4. Normal Form

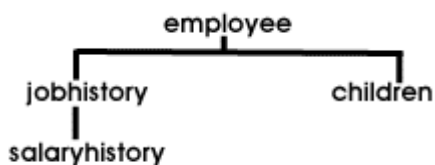
A relation whose domains are all simple can be represented in storage by a two-dimensional column-homogeneous array of the kind discussed above. Some more complicated data structure is necessary for a relation with one or more nonsimple domains. For this reason (and others to be cited below) the possibility of eliminating nonsimple

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domains appears worth investigating. [see [note 4](#)] There is, in fact, a very simple elimination procedure, which we shall call normalization.

Consider, for example, the collection of relations exhibited in [figure 3\(a\)](#). *Job history* and *children*, are nonsimple domains of the relation *employee*. *Salary history* is a nonsimple domain of the relation *job history*. The tree in [figure 3\(a\)](#) shows just these interrelationships of the nonsimple domains.



employee (*man#*, name, birthdate, jobhistory, children)

jobhistory (*jobdate*, title, salaryhistory)

children (*salarydate*, salary)

children (*childname*, birthyear)

Figure 3(a). Unnormalized set

employee' (*man#*, name, birthdate)

jobhistory' (*man#*, jobdate, title)

salaryhistory' (*man#*, jobdate, salarydate, salary)

children' (*man#*, childname, birthyear)

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Figure 3(b). Normalized Set

Normalization proceeds as follows. Starting with the relation at the top of the tree, take its primary key and expand each of the immediately subordinate relations by inserting this primary key domain or domain combination. The primary key of each expanded relation consists of the primary key before expansion augmented by the primary key copied down from the parent relation. Now, strike out from the parent relation all nonsimple domains, remove the top node of the tree, and repeat the same sequence of operations on each remaining subtree.

The result of normalizing the collection of relations in [Figure 3\(a\)](#) is the collection in [Figure 3\(b\)](#). The primary key of each relation is italicized to show how such keys are expanded by the normalization.

If normalization as described above is to be applicable, the unnormalized collection of relations must satisfy the following conditions:

1. The graph of interrelationships of the nonsimple domains is a collection of trees
2. No primary key has a component domain which is nonsimple.

The writer knows of no application which would require any relaxation of these conditions.

Further operations of a normalizing kind are possible. These are not discussed in this paper.

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The simplicity of the array representation which becomes feasible when all relations are cast in normal form is not only an advantage for storage purposes but also for communication of bulk data between systems which use widely different representations of the data. The communication form would be a suitably compressed version of the array representation and would have the following advantages:

1. It would be devoid of pointers (address-valued or displacement-valued). It would avoid all dependence on hash addressing schemes.
2. It would contain no indices or ordering lists.

If the user's relational model is set up in normal form, names of items of data in the data bank can take a simpler form than would otherwise be the case. A general name would take a form such as

R(g).r.d

where R is a relational name; g is a generation identifier (optional); r is a role name (optional); d is a domain name. Since g is needed only when several generations of a given relation exist, or are anticipated to exist, and r is needed only when the relation R has two or more domains named d, the simple form R.d will often be adequate.

1.5. Some Linguistic Aspects

The adoption of a relational model of data, as described above, permits the development of a universal data sublanguage based on an applied predicate calculus. A first-order

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predicate calculus suffices if the collection of relations is in normal form. Such a language would provide a yardstick of linguistic power for all other proposed data languages, and would itself be a strong candidate for embedding. (with appropriate syntactic modification) in a variety of host languages (programming, command-, or problem-oriented). While it is not the purpose of this paper to describe such a language in detail, its salient features would be as follows.

Let us denote the data sublanguage by R and the host language by H . R permits the declaration of relations and their domains. Each declaration of a relation identifies the primary key for that relation. Declared relations are added to the system catalog for use by any members of the user community who have appropriate authorization. H permits supporting declarations which indicate, perhaps less permanently, how these relations are represented in storage. R permits the specification for retrieval of any subset of data from the data bank;. Action on such a retrieval request is subject to security constraints.

The universality of the data sublanguage lies in its descriptive ability (not its computing ability). In a large data bank each subset of the data has a very large number of possible (and sensible) descriptions, even when we assume (as we do) that there is only a finite set of function subroutines to which the system has access for use in qualifying data for retrieval. Thus, the class of qualification expressions which can be used in a set specification must have the descriptive power of the class of well-formed formulas of an applied predicate calculus. It is well known that to preserve this descriptive power it is

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unnecessary to express (in whatever syntax is chosen) every formula of the selected predicate calculus. For example, just those in prenex normal form are adequate [9].

Arithmetic functions may be needed in the qualification or other parts of retrieval statements. Such functions can be defined in H and invoked in R .

A set so specified may be fetched for query purposes only, or it may be held for possible changes. Insertions take the form of adding new elements to declared relations without regard to any ordering that may be present in their machine representation. Deletions which are effective for the community (as opposed to the individual user or subcommunities) take the form of removing elements from declared relations. Some deletions and updates may be triggered by others, if deletion and update dependencies between specified relations are declared in R .

One important effect that the view adopted toward data has on the language used to retrieve it is in the naming of data elements and sets. Some aspects of this have been discussed in the previous section. With the usual network view, users will often be burdened with coining and using more relation names than are absolutely necessary, since names are associated with paths (or path types) rather than with relations.

Once a user is aware that a certain relation is stored, he will expect to be able to exploit [see [note 5](#) using any combination of its arguments as "knows" and the remaining arguments as "unknowns," because the information (like Everest) is there. This is a system feature (missing from many current information systems) which we shall call (logically)

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symmetric exploitation of relations. Naturally, symmetry in performance is not to be expected.

To support symmetric exploitation of a single binary relation, two directed paths are needed. For a relation of degree n , the number of paths to be named and controlled is n factorial.

Again, if a relational view is adopted in which every n -ary relation ($n > 2$) has to be expressed by the user as a nested expression involving only binary relations (see Feldman's LEAP System [10], for example) then $2n - 1$ names have to be coined instead of only $n + 1$ with direct n -ary notation as described in [Section 1.2](#). For example, the 4-ary relation *supply* of [Figure 1](#), which entails 5 names in n -ary notation, would be represented in the form

P (supplier, Q (part, R (project, quantity)))

in nested binary notation and, thus, employ 7 names.

A further disadvantage of this kind of expression is its asymmetry. Although this asymmetry does not prohibit symmetric exploitation, it certainly makes some bases of interrogation very awkward for the user to express (consider, for example, a query for those parts and quantities related to certain given projects via Q and R).

1.6. Expressable, Names, and Stored Relations

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Associated with a data bank are two collections of relations: the *named set* and the *expressible set*. The named set is the collection of all those relations that the community of users can identify by means of a simple name (or identifier). A relation R acquires membership in the named set when a suitably authorized user declares $R \langle /E \rangle$; it loses membership when a suitably authorized user cancels the declaration of R .

The *expressible set* is the total collection of relations that can be designated by expressions in the data language. Such expressions are constructed from simple names of relations in the named set; names of generations, roles and domains; logical connectives; the qualifiers of the predicate calculus; [see [note 6](#)] and certain constant relation symbols such as $=$, $>$. The named set is a subset of the expressible set - usually a very small subset.

Since some relations in the named set may be time-independent combinations of others in that set, it is useful to consider associating with the named set a collection of statements that define these time-independent constraints. We shall postpone further discussion of this until we have introduced several operations on relations (see Section 2).

One of the major problems confronting the designer of a data system which is to support a relational model for its users is that of determining the class of stored representations to be supported. Ideally, the variety of permitted data representations should be just adequate to cover the spectrum of performance requirements of the total collection of installations. Too

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great a variety leads to unnecessary overhead in storage and continual reinterpretation of descriptions for the structures currently in effect.

For any selected class of stored representations the data system must provide a means of translating user requests expressed in the data language of the relational model into corresponding and efficient actions on the current stored representation. For a high level data language this presents a challenging design problem. Nevertheless, it is a problem which must be solved as more users obtain concurrent access to a large data bank, responsibility for providing efficient response- and throughput shifts from the individual user to the data system.

Notes

2

In mathematical terms, A relationship is an equivalence class of those relations that are equivalent under permutation of domains (see Section 2.1.1).

3 Naturally, as with any data put into and retrieved from a computer system, the user will normally make far more effective use of the data if he is aware of its meaning.

4

M. E. Sanko of IBM, San Jose, independently recognized the desirability of eliminating nonsimple domain.

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5

Exploiting a relation includes query, update, and delete.

6

Because each relation in a practical data bank is a finite set nt every instnnt of time, the existential and universal quantifiers can be expressed in terms of a function that counts the number of elements in a any finite set.

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